

A Linear Active Disturbance Rejection Controller-Based Sensorless Control Scheme for PMSM Drives

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Abstract—Sliding-mode observer (SMO)-based rotor position sensorless field-oriented control (FOC) methods have been widely employed for permanent-magnet synchronous motor (PMSM) drives used in electric vehicles. However, these methods have two main problems: phase delay and speed chattering. To cope with these two issues, a linear active disturbance rejection controller (LADRC)-based sensorless FOC scheme is proposed in this paper. The LADRC consists of a linear extended state observer (LESO) and a proportional current controller. The LESO is designed to estimate the back electromotive force (EMF) of the PMSM, which is treated as the external disturbance, without using any low-pass filter or switching function. Then, the rotor position and speed are obtained from the estimated back EMF without any phase delay or speed chattering problem. The estimated disturbance is used as a feedforward compensation term for the input of the plant. The plant combined with the LESO is equivalent to a zero-pole first-order system with a unity gain, which is controlled by a simple proportional current controller to generate the desired voltage vector for the pulse-width modulation (PWM) control of the PMSM inverter. The proposed LADRC-based sensorless FOC scheme is validated by both simulation and experimental results for a 275-W salient-pole PMSM drive in which the PMSM is similar to the traction motor used in Toyota Prius hybrid electric vehicles at a reduced scale.

Keywords—Field oriented control (FOC), linear active disturbance rejection control (LADRC), linear extended state observer (LESO), permanent-magnet synchronous motor (PMSM), rotor position estimation, sensorless control.

I. INTRODUCTION

Permanent-magnet synchronous motors (PMSMs) have been widely employed in industrial applications owing to their high reliability, high efficiency, and high power density [1], [2]. To achieve high-performance control for PMSMs, electromechanical sensors, such as hall-effect sensors, optical encoders, and resolvers are commonly used. However, the use of these sensors not only increases the cost but also reduces the reliability of the PMSM drive systems [3]. Therefore, sensorless FOC of PMSM drives has been widely researched in the last few decades.

The sensorless FOC methods for salient-pole PMSMs can be generally classified into two categories: the high-frequency

(HF) signal injection methods and the back electromotive force (EMF) estimation methods. For zero- and low-speed operations, the HF signal injection methods were well founded and exhibited satisfying performance [4], [5]. However, their capability of estimating the rotor position deteriorates dramatically in medium- to high-speed operations due to the limited control bandwidth.

The EMF estimation methods, by contrast, perform well in medium- and high-speed operations by observing the back EMF [6], [7]. The main technologies for the EMF observation include the direct calculation [8], the reduced-order extended Kalman filter (EKF) [9], and the sliding-mode observer (SMO) [7]. The direct calculation method is simple but is susceptible to machine parameter variations and sampling noise. Compared to the direct calculation method, the sampling noise can be eliminated and more accurate rotor position and speed estimation results can be obtained by using the reduced-order EKF method. However, the computational burden of the EKF method is heavier. Due to its simple algorithm and strong robustness to machine parameter variations, the SMO method has attracted more and more attention, especially in the applications of traction motor drives for hybrid electric vehicles. The defects of the SMO method are the speed chattering and phase delay problems. Plenty of work has been done to solve these two problems, such as using the sigmoid function instead of the sign function [10] and phase compensation [11]. However, the problems have not been completely solved. To solve the two problems completely, a disturbance observer [12] was proposed to estimate the back EMF. However, it is hard to design the gains of the disturbance observer due to the variations of the machine parameters used in the observer.

Recently, a method called active disturbance rejection control (ADRC) has been applied in motor drive systems [13], [14] because its design process does not rely on an accurate mathematical model of the system and it has a strong disturbance rejection capability. A robust control method that employed three first-order ADRCs was proposed for the speed control of an induction motor drive, which removed the need for the rotor flux estimation and reduced the computation burden [13]. In [14], an ADRC was combined with a model

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predictive control for the speed loop of a PMSM drive system to enhance the system robustness to disturbances, including machine parameter variations and external load changes. However, little work has been reported on the application of the ADRC for position sensorless control of PMSM drives.

This paper proposes a novel linear ADRC (LADRC)-based rotor position sensorless FOC scheme for PMSM drives in an estimated synchronously rotating reference frame. The LADRC consists of a linear extended state observer (LESO) and a proportional current controller. The LESO is designed to estimate the back EMF, which is treated as an external disturbance, without using any low-pass filter or switching function. Then, the rotor position and speed are obtained from the estimated back EMF by using a tracking controller without any phase delay or speed chattering problem. The estimated disturbance, i.e., back EMF, is also used to compensate the input of the plant. In this way, the plant combined with the LESO is equivalent to a zero-pole first-order system, which can be controlled by a simple proportional current controller to generate the desired voltage vector for the PWM control of the PMSM inverter. The effectiveness of the LADRC-based sensorless FOC scheme is evaluated by both simulation and experimental results for a 275-W salient-pole PMSM drive.

II. PROPOSED LADRC-BASED ROTOR POSITION SENSORLESS FOC SCHEME FOR PMSM DRIVES

A. Problem of the SMO-based Sensorless FOC for a PMSM

For a salient-pole PMSM, a back EMF-based model is commonly used, which can be written in a stationary $\alpha\beta$ reference frame according to [3] as follows:

$$\begin{bmatrix} v_{s\alpha} \\ v_{s\beta} \end{bmatrix} = \begin{bmatrix} R_s + pL_d & \omega_{re}(L_d - L_q) \\ \omega_{re}(L_q - L_d) & R_s + pL_d \end{bmatrix} \begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \end{bmatrix} + \eta \begin{bmatrix} -\sin \theta_{re} \\ \cos \theta_{re} \end{bmatrix} \quad (1)$$

where $v_{s\alpha}$ and $v_{s\beta}$ are the α - and β -axis stator voltages, respectively; $i_{s\alpha}$ and $i_{s\beta}$ are the α - and β -axis stator currents, respectively; R_s is the stator armature resistance; L_d and L_q are the d - and q -axis inductances, respectively; ω_{re} is the rotor electrical angular speed; $p = d/dt$ is the time derivative operator; θ_{re} is the rotor position angle; and η is the magnitude of the back EMF, and can be written as:

$$\eta = (L_d - L_q)(\omega_{re} i_{sd} - p i_{sq}) + \omega_{re} \psi_m \quad (2)$$

where i_{sd} and i_{sq} are the d - and q -axis stator currents, respectively; and ψ_m is the rotor magnet flux linkage.

The last term on the right-hand side of (1) contains the information of the rotor position, and is called the back EMF. If the back EMF can be estimated by an observer, then the rotor position can be extracted by using an inverse tangent method or an angle tracking observer.

Among various types of observers, the SMO is a promising candidate for the back EMF estimation due to its simple algorithm and high robustness to the disturbance. The mathematical formulation of the SMO is expressed as:

$$\begin{cases} p\hat{i}_{s\alpha} = \frac{v_{s\alpha}}{L_d} - \frac{R_s}{L_d}\hat{i}_{s\alpha} + \hat{\omega}_{re} \frac{L_q - L_d}{L_d} i_{s\beta} + lZ_{\alpha} \\ p\hat{i}_{s\beta} = \frac{v_{s\beta}}{L_d} - \frac{R_s}{L_d}\hat{i}_{s\beta} + \hat{\omega}_{re} \frac{L_d - L_q}{L_d} i_{s\alpha} - lZ_{\beta} \end{cases} \quad (3)$$

where l is the observer gain; Z_{α} and Z_{β} are the α - and β -axis outputs of the sign functions, respectively; and $\hat{\omega}_{re}$ is the estimated rotor electrical angular speed. In practice, two low-pass filters are used after the outputs of the two sign functions to obtain the back EMF. Then, the rotor position can be obtained from the estimated back EMF by using a phase-locked loop (PLL). Fig. 1 shows the block diagram of the conventional SMO-based rotor position estimation method for the salient-pole PMSM. The low-pass filters need to be designed properly to mitigate the oscillating position error due to the unwanted noise caused by the sign function.

Due to the use of the low-pass filters, there is a phase delay in the estimated back EMF. Moreover, there is a speed chattering problem in the estimated back EMF due to the use of the discrete sign functions. These two problems usually make the system performance unsatisfactory. To solve the problems of the SMO-based rotor position estimation method, this paper proposes a LESO-based rotor position estimation method, as described in the next subsection.

B. Proposed LADRC-Based Sensorless FOC for a PMSM

A back EMF-based model for a salient-pole PMSM can be written in the synchronously rotating dq reference frame as follows:

$$\begin{bmatrix} v_{sd} \\ v_{sq} \end{bmatrix} = \begin{bmatrix} R_s + pL_d & -\omega_{re} \cdot L_q \\ \omega_{re} \cdot L_q & R_s + pL_d \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{sq} \end{bmatrix} + \begin{bmatrix} 0 \\ \eta \end{bmatrix} \quad (4)$$

where v_{sd} and v_{sq} are the d - and q -axis stator voltages, respectively.

However, in a sensorless drive system, such a dq model cannot be utilized since the rotor position θ_{re} is not measured. To solve this problem, an estimated synchronously rotating $\gamma\delta$ reference frame instead of the actual synchronously rotating dq reference frame is used, as shown in Fig. 2. Then, a rotor position estimation error $\Delta\theta_{re}$ is defined as:

$$\Delta\theta_{re} = \hat{\theta}_{re} - \theta_{re} \quad (5)$$

where $\hat{\theta}_{re}$ is the rotor position estimated in the $\gamma\delta$ reference frame.

By transforming (4) into the $\gamma\delta$ reference frame, the back

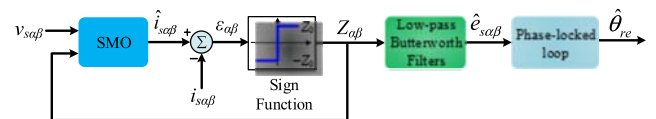


Fig. 1. Block diagram of the SMO-based rotor position estimation for the salient-pole PMSM.

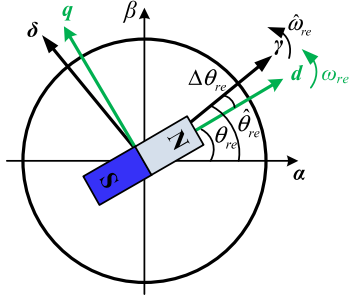


Fig. 2. The estimated $\gamma\delta$ reference frame and the dq reference frame.

EMF-based PMSM model can be expressed as:

$$\begin{bmatrix} v_{s\gamma} \\ v_{s\delta} \end{bmatrix} = \begin{bmatrix} R_s + pL_d & -\hat{\omega}_{re} \cdot L_q \\ \hat{\omega}_{re} \cdot L_q & R_s + pL_d \end{bmatrix} \begin{bmatrix} i_{s\gamma} \\ i_{s\delta} \end{bmatrix} + \begin{bmatrix} e_{s\gamma} \\ e_{s\delta} \end{bmatrix} \quad (6)$$

where $v_{s\gamma}$ and $v_{s\delta}$ are the γ - and δ -axis stator voltages, respectively; $i_{s\gamma}$ and $i_{s\delta}$ are the γ - and δ -axis stator currents, respectively; and $e_{s\gamma}$ and $e_{s\delta}$ are the γ - and δ -axis back EMF components, respectively, which can be expressed as:

$$\begin{bmatrix} e_{s\gamma} \\ e_{s\delta} \end{bmatrix} = \eta \begin{bmatrix} -\sin \Delta\theta_{re} \\ \cos \Delta\theta_{re} \end{bmatrix} + (\hat{\omega}_{re} - \omega_{re}) \cdot L_q \begin{bmatrix} -i_{s\gamma} \\ i_{s\delta} \end{bmatrix} \quad (7)$$

If $\hat{\omega}_{re} \approx \omega_{re}$, $\Delta\theta_{re}$ can be calculated as $\Delta\theta_{re} = -\tan^{-1}(e_{s\gamma}/e_{s\delta})$ according to (7). Moreover, if $e_{s\gamma}/L_d$ and $e_{s\delta}/L_d$ are treated as the γ - and δ -axis unknown external disturbances $f_{e\gamma}$ and $f_{e\delta}$, respectively, which contain the information of the γ - and δ -axis back EMF components and rotor position estimation error, the current model of the salient-pole PMSM can be written as:

$$\begin{cases} p i_{s\gamma} = v_{s\gamma} / L_d + f_{e\gamma} - f_{e\delta} \\ p i_{s\delta} = v_{s\delta} / L_d + f_{e\delta} - f_{e\gamma} \end{cases} \quad (8)$$

where $f_{e\gamma} = \hat{\omega}_{re} \cdot L_q \cdot i_{s\delta} / L_d - R_s \cdot i_{s\gamma} / L_d$ and $f_{e\delta} = -\hat{\omega}_{re} \cdot L_q \cdot i_{s\gamma} / L_d - R_s \cdot i_{s\delta} / L_d$, which represent the γ - and δ -axis known model information, respectively.

Then, a LESO-based external disturbance observer can be designed as:

$$\begin{cases} p \hat{i}_{sx} = v_{sx} / L_d + f_x - \hat{f}_{e_x} - L_{x1} \cdot \varepsilon_x \\ p \hat{f}_{e_x} = -L_{x2} \varepsilon_x \end{cases} \quad x = \gamma \text{ and } \delta \quad (9)$$

where \hat{i}_{sx} is the estimated stator current; $\varepsilon_x = \hat{i}_{sx} - i_{sx}$ is the stator current estimation error; \hat{f}_{e_x} is the estimated unknown external disturbance; and L_{x1} and L_{x2} are the gains of the LESO. The values of L_{x1} and L_{x2} can be determined according to the desired bandwidth of the LESO [15], which should be large enough to ensure that the dynamics of the LESO is

sufficiently fast to track the variation of the disturbance. For example, the values of L_{x1} and L_{x2} can be simply determined such that the tracking error state equation of the LESO has the desired bandwidth.

Then, a tracking controller [16] can be designed to estimate the rotor position and speed by simply using a PLL to regulate the normalized value of the estimated γ -axis unknown external disturbance \hat{f}_{e_γ} , which contains the rotor position error information, to be zero, as shown in Fig. 3. The normalization of the back EMF components guarantees a constant linear dynamic response of the tracking controller regardless of the operating fundamental frequency.

According to the ADRC theory [17], the estimated disturbance is used as a feedforward compensation term for the input of the plant, as shown in Fig. 4. The combination of the plant and the LESO is equivalent to a zero-pole first-order system $1/s$ in the Laplace domain. Then, a simple proportional current controller k_{px} can be designed to generate the voltage output v_{sx0} , which is compensated by the disturbance estimated by the LESO to generate the voltage output v_{sx} of the LADRC, i.e., $v_{sx} = v_{sx0} - L_d(\hat{f}_{e_x} + f_x)$, for controlling the plant.

Compared to the conventional SMO-based method, there are two improvements in the proposed LESO-based rotor position estimation scheme. Firstly, by applying the estimated synchronously rotating reference frame instead of the stationary reference frame in the SMO-based method, the back EMF is transformed into DC components, which removes the need for the low-pass filter and, therefore, eliminates the phase delay in the estimated position. Secondly, due to the use of a continuous integrator $1/s$ in the LESO to estimate the back EMF components, the speed chattering problem caused

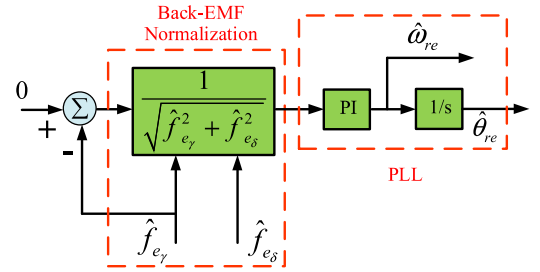


Fig. 3. Block diagram of the tracking controller for rotor position and speed estimation.

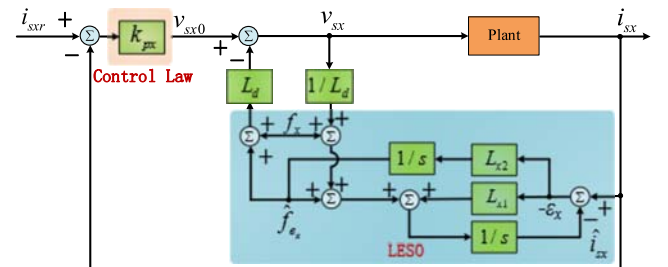


Fig. 4. Block diagram of the plant controlled by the LADRC scheme.

was proposed for PMSM drive systems in an estimated synchronously rotating reference frame. The proposed sensorless FOC resolved the phase delay and speed chattering problems in the conventional SMO-based sensorless FOC schemes. The performance of the proposed LADRC-based sensorless FOC scheme was validated by both simulation and experimental results for a 275-W salient-pole PMSM drive. The simulation and experimental results showed that the PMSM drive using the LADRC-based scheme was not affected by PMSM parameter mismatches at all and had better rotor position estimation performance than the conventional SMO-based sensorless FOC scheme.

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